## Mathematics Album

## Early Work - Numeration

Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration
Mathematics: Early Work - Numeration

## Operations

Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations
Mathematics: Operations

Squares and Cubes of Numbers
Mathematics: Squares and Cubes
Mathematics: Squares and Cubes
Mathematics: Squares and Cubes
Mathematics: Squares and Cubes
Mathematics: Squares and Cubes
Mathematics: Squares and Cubes

## Fractions

Mathematics: Fractions
Mathematics: Fractions
Mathematics: Fractions
Mathematics: Fractions

## Great Lesson: Story of Numbers

Wooden Hierarchical Material
Large Bead Frame
Commutative and Distributive Laws of Multiplication Multiples
start "end" additional notes/pre-requisites

Factors - 1: Introduce Concept
Least Common Multiples - 1: Introduction
Last Steps of Least Common Multiples to Abstraction
Divisibility: by 2, 5, 25 (3 presentations)

Large Bead Frame Long Mult
Bank Game
Flat Bead Frame - Step 1
Checker Board
Geometrical Form of Multiplication
Category Multiplication
Long Division (Distributive) Racks and Tubes
Group Division
Group Division \& Word Problems

Prerequisites to Squares and Cubes of Numbers
Notation of Squares
Notation of Cubes
Games 1-4 (pyramid, tower, decanomial square)
Paper Decanomial
Sums Using Squares and Cubes

Introduction to Fractions (many stages)
Equivalence of Fractions (stages)
Simple Operations
Add \& Subt of Fraction w/ Diff Denominators

1
1
2
3
repeat yearly

1 bridge from golden bead
1 start where child is parallel - bead frame
1
1
2
2 Factors confidence
2

1
3 (this is with cards, NOT with beads)
2 large bead frame mult done
2
3 after checkerboard
3 could be 1st year
3 1-digit divisor experience
4 Comfort with Long Div
5

3
3

11 could have had in primary; add more details
11 follow the child
2 could have had in primary; build
2 pre-req: add/sub simple

Mathematics: Fractions
Mathematics: Fractions
Mathematics: Fractions

## Decimal Fractions

Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions
Mathematics: Decimal Fractions

## Squaring and Cubing

Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing
Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing Mathematics: Squaring and Cubing
Mathematics: Squaring and Cubing

| Exercises Leading to Abstraction of the Above | 2 | 3 |
| :--- | :--- | :--- |
| Multiplication by Fraction (stages) | 2 | 3 can be year 1 |
| Division by a Fraction | 2 | 3 |

3 can be year 1
3

Quantity - Symbol - Link
Operations
Convert Common to Decimal Fractions
Effects of Mult or Div by Powers of 10
Multiplying a DF by a DF - Ex 1: 1-digit multiplier
Decimal Checkerboard
Relative Size of Terms/Numbers
Division of a Decimal Fraction by a Decimal Fraction
Leading to Abstraction of Multiplication of Decimal Fractions
Division of a Decimal Fraction on Paper

Transformation of a Square
Passing From One Square to Another
Squaring a Sum: Binomial - Trinomial - Formula
Squaring with a Hierarchical Value: stages
Pass From One Cube to Another
Cubing a Binomial
Cubing a Trinomial
Cubing a Quadrinomial
Cubing a Trinomial having Numerical Value
The Story of the Three Kings
Cubing a Number with Decimal Value
Square Roots
Square Roots - Abstraction stages
Special Cases - stages
Square Roots: review process and rules
Cube Roots
Cube Roots: Review concept and rule

Signed Numbers: Negative Snake Game

Signed Numbers: Operations (stages)

3 see page for pre-reqs
3
3

3
3
3
5
4
5
5

3 parallel with later multiples and factors
3
3
4
4 beginnings overlap with square work
4
5
5
4
4
4
4
5
5
6
5
6

## Other Topics

Mathematics: Signed Numbers
Mathematics: Signed Numbers

NOTE: Much of this area depends on the child 4 NOTE 2: Anything 4-6 could start in year 5 6

Mathematics: Powers of Numbers
Mathematics: Powers of Numbers
Mathematics: Powers of Numbers
Mathematics: Powers of Numbers
Mathematics: Powers of Numbers
Mathematics: Powers of Numbers
Mathematics: Word Problems
Mathematics: Word Problems
Mathematics: Word Problems
Mathematics: Other Number Bases
Mathematics: Other Number Bases
Mathematics: Algebra
Mathematics: Algebra
Mathematics: Algebra
Mathematics: Algebra
Mathematics: Ratio and Proportion

Powers of 2
Powers of 3: Full work 46
Powers of 2 and 3: Combined 46
Powers of $10 \quad 4 \quad 6$
Operations Using Exponential Notation 4
Expanded Power Notation - Intro and Operations 46
Word Problems
Distance/Velocity/Time
Principal/Interest/Rate/Time
Non-Decimal Bases: Intro and Operations
Conversion of Number Bases
Balancing an Equation using operations
Solve for Unknown: Operations
Algebra Word Problems
Solve for Two Unknowns
All stages in upper elementary typically

16 Introduce early on with concrete materials
4 be sure to begin before end of year 3
5
6 Follow the child's interests to start sooner
6
6
6
6
6
6
6

6
46
46 later work could extend into lower adolescence

